

$$\beta : (\widehat{Loc} \rightarrow \widehat{Loc}) \rightarrow (\widehat{State} \rightarrow \widehat{State})$$